

wage

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_1^2 + u$$

$\beta_1 + 2\beta_2 \text{educ.}$

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_1 \cdot x_2 + u$$

wage

$\beta_1 + \beta_3 \text{exper.}$

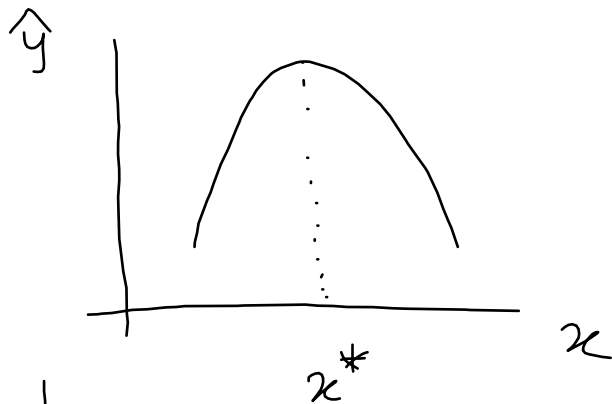
Ch. 6

Quadratic Functions

$$y = \beta_0 + \beta_1 x + \beta_2 x^2 + u$$

$$\frac{\Delta y}{\Delta x} = \beta_1 + 2\beta_2 x$$

$$\hat{\beta}_1 > 0, \hat{\beta}_2 < 0$$



Turning pt. (max.)

$$\text{at } x^* = \left| \frac{\hat{\beta}_1}{2\hat{\beta}_2} \right|$$

BWGH12

$$\text{bwght} = \beta_0 + \beta_1 \text{mage} + \beta_2 \text{mage}^2 + u$$

$$\hat{\beta}_1 = 97.36$$

$$\hat{\beta}_2 = -1.57$$

$$\frac{\Delta \text{bwght}}{\Delta \text{mage}} = \beta_1 + 2\beta_2 \text{mage}$$

$$\text{at } \text{mage} = 25 : 97.36 + 2(-1.57)25 = 18.86$$

$$\text{" } = 40 : \text{" } 40 = -28.24$$

$$\text{mage}^* = \left| \frac{97.36}{2(-1.57)} \right| = 31.03 \text{ yrs.}$$

. reg bwght mage magesq

Source	SS	df	MS	Number of obs	=	1,832
Model	5089853.55	2	2544926.78	F(2, 1829)	=	7.71
Residual	603540921	1,829	329984.101	Prob > F	=	0.0005
				R-squared	=	0.0084
				Adj R-squared	=	0.0073
Total	608630775	1,831	332403.481	Root MSE	=	574.44

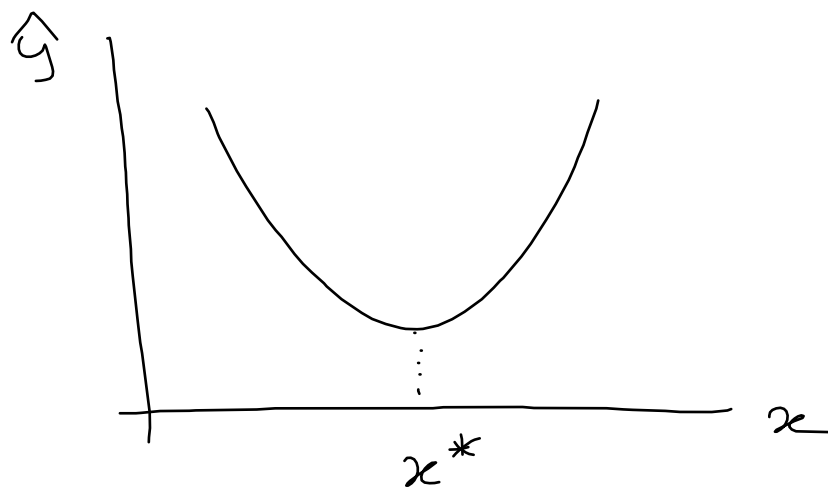
	Coefficient	Std. err.	t	P> t	[95% conf. interval]	
mage	97.35971	25.7041	3.79	0.000	46.94724	147.7722
magesq	-1.568884	.429678	-3.65	0.000	-2.411595	-.7261728
_cons	1929.752	379.4908	5.09	0.000	1185.471	2674.033

. di "Turning point = " abs(_b[mage]/(2*_b[magesq]))
Turning point = 31.028334

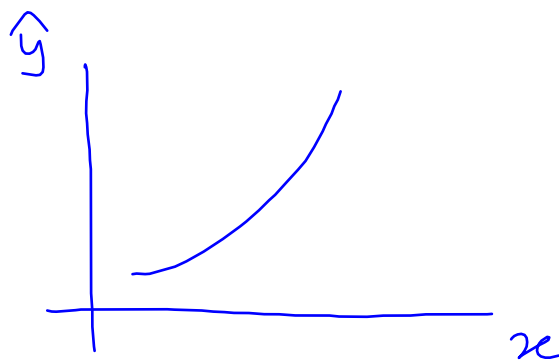
$$\hat{\beta}_1 < 0 \quad \& \quad \hat{\beta}_2 > 0$$

Turning pt. (min.)

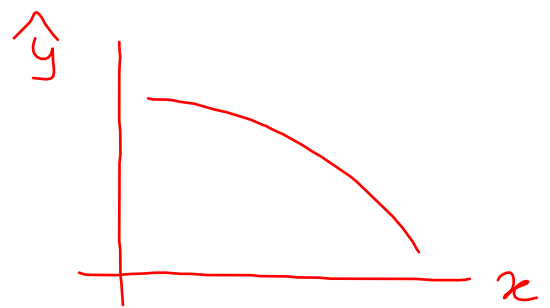
$$\text{at } x^* = \left| \frac{\hat{\beta}_1}{2\hat{\beta}_2} \right|$$



$$\hat{\beta}_1 > 0 \quad \& \quad \hat{\beta}_2 > 0$$



$$\hat{\beta}_1 < 0 \quad \& \quad \hat{\beta}_2 < 0$$



Interaction Terms

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_1 \cdot x_2 + u$$

$$\frac{\Delta y}{\Delta x_1} = \beta_1 + \beta_3 x_2$$

e.g. $\frac{\Delta y}{\Delta x_1}$ at $x_2 = \bar{x}_2$

$$\frac{\Delta y}{\Delta x_2} = \beta_2 + \beta_3 x_1$$

$$\hat{\beta}_1 + \hat{\beta}_3 \bar{x}_2$$

$$\text{bwght} = \beta_0 + \beta_1 \text{mage} + \beta_2 \text{npvis} + \beta_3 \text{mage} \times \text{npvis} + u$$

$$\hat{\beta}_1 = 28.65 \quad \hat{\beta}_2 = 78.98 \quad \hat{\beta}_3 = -2.2$$

$$\frac{\Delta \text{bwght}}{\Delta \text{mage}} = \beta_1 + \beta_3 \text{npvis} \rightarrow \text{avg.} = 11.62$$

$$\text{at } \bar{\text{npvis}} : 28.65 - 2.2 \times 11.62 = 3.086$$

Ch. 7

Dummy / binary indep. var.

y	x	u
trade/ env. performance	trade/env. agreement	political pref.
wage	marital status	work ethic, reliability

Single Dummy Variable:

$$y = \beta_0 + \delta_0 x + u$$

↓
0/1

$$E(y|x) = \beta_0 + \delta_0 x$$

$$\Rightarrow \delta_0 = E(y|x=1) - E(y|x=0)$$

effect
of $x=1$ rel. to
 $x=0$ (base/
reference
group)

$$\hat{\delta}_0 = \bar{y}_{x=1} - \bar{y}_{x=0}$$

$= \overline{\text{wage}}_{\text{marr.}} - \overline{\text{wage}}_{\text{not.marr.}}$

if $y \rightarrow$ wage
 $x \rightarrow 1$ for marr.
0 for not "