

## Ch: 4 Inference

$\beta \rightarrow$  unknown  
test e.g.  $\beta = 0$  using  $\hat{\beta}$

3 ways of testing

┌ is  $\hat{\beta}$  too far from hypothesized  $\beta$   
├ how improbable is  $\hat{\beta}$   
└ is  $\beta$  in  $\hat{\beta} - E, \hat{\beta} + E$

## Sampling Distributions

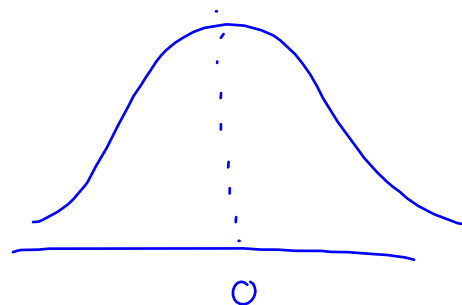
$$\hat{\beta}_j = \beta_j + \text{a term linear in } u$$

↓

its distribution follows from  
that of  $u$

Ass<sup>n</sup>:  $u$  indep. of  $(x_1, \dots, x_k)$   
↳ normal  $E(u) = 0$   
 $\text{var}(u) = \sigma^2$

$$u \sim N(0, \sigma^2)$$



Given all the ass<sup>n</sup>s  
up to normality

$$\hat{\beta}_j \sim N(\beta_j, \text{var}(\hat{\beta}_j))$$

↳ derived in  
ch. 3

$$\frac{\hat{\beta}_j - \beta_j}{\text{sd}(\hat{\beta}_j)} \sim N(0, 1)$$

$$\text{sd}(\hat{\beta}_j)$$

$$\frac{\hat{\beta}_j - \beta_j}{\text{se}(\hat{\beta}_j)} \sim t_{n-k-1} \quad (t \text{ dist. with } df = n-k-1)$$

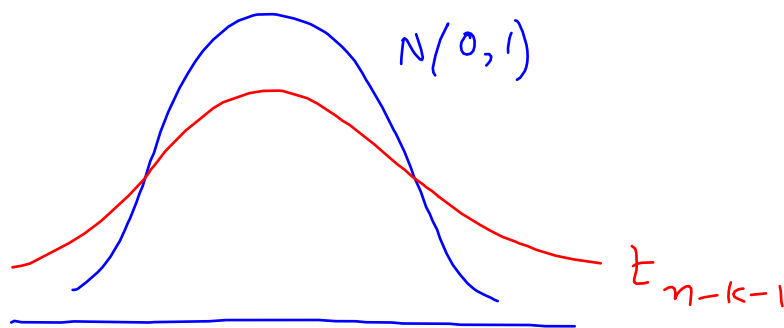
→  $N(0, 1)$  as  $df \rightarrow \infty$

↓  
using  $\hat{\sigma}$  instead of  $\sigma$

Recap of

Regression ass<sup>n</sup>s (prior to normality)

- ① Linear in  $\beta$ 's
- ② Random sample
- ③ Variation in  $x$   
 $x_1, x_2, \dots, x_n$ : not linearly related
- ④  $u$  &  $x$  → not correlated
- ⑤ Homoskedasticity



## Single Hypothesis — Single Parameter

Null  $H_0 : \beta_j = a_j$

$a_j = 0 \rightarrow$  special case

Alternative  $H_1 : \beta_j \neq a_j$