



Chapter 5

consistency:

No asymptotic bias under slightly weaker assumptions.

$$E(u) = 0$$

$$\text{corr.}(x, u) = 0$$

For unbiased $\hat{\beta} \rightarrow$ as $n \uparrow$ dist. of $\hat{\beta}$ more concentrated around β .

$$\sigma^2 : \quad \frac{SSR}{n - (k+1)} \quad \frac{SSR}{n-2} \rightarrow \text{unbiased estimator of } \sigma^2$$

$$\frac{SSR}{n} \rightarrow \text{biased but consistent estimator of } \sigma^2$$

Asymptotic Normality:

$u \rightarrow \text{Normal}$

$y \mid x_1, x_2, x_3, \dots, x_k \rightarrow \text{Normal}$

often not the case.

e.g. $y \rightarrow$ indicator of employment
cigs., # kids

Under the ass^{ns} for unbiasedness &
homoskedasticity

$\overset{a}{\sim}$: asymptotically
distributed
as

$$\frac{\hat{\beta}_j - \beta_j}{\text{se}(\hat{\beta}_j)} \overset{a}{\sim} \text{Normal}(0, 1)$$
$$\sim t_{n-k-1}$$

F statistics also have approximate F dist.
with large n .

Chapter 6

Quadratic functions

$$y = \beta_0 + \beta_1 x + \beta_2 x^2 + u$$

$$\frac{\Delta y}{\Delta x} = \beta_1 + 2\beta_2 x$$

Δx

$$\hat{\beta}_1 > 0, \hat{\beta}_2 < 0$$

Turning pt. (max.)

$$\text{at } x^* = \left| \frac{\hat{\beta}_1}{2\hat{\beta}_2} \right|$$

