

Ch.: 4 (Inference)

$\beta \rightarrow$ unknown
test using $\hat{\beta}$

3 ways

- is $\hat{\beta}$ far away from hyp. value of β
- how improbable is $\hat{\beta}$
- is hyp. β in $\hat{\beta} - E, \hat{\beta} + E$
↓
margin of error

Sampling Distribution

$$\hat{\beta}_j = \beta_j + \text{a term linear in } u$$



its distribution follows from that of u

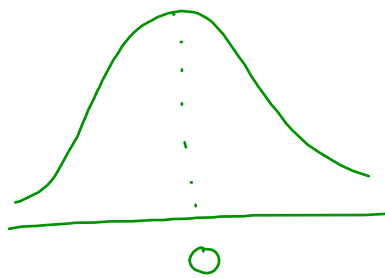
Assⁿ: $u \rightarrow$ indep. of $x_1 \dots x_k$
↳ normal

$$u \sim N(0, \sigma^2)$$

is distributed as

↓
 $E(u) = 0$

→ $\text{var}(u) = \sigma^2$



$$\hat{\beta}_j \sim N(\beta_j, \text{var}(\hat{\beta}_j))$$

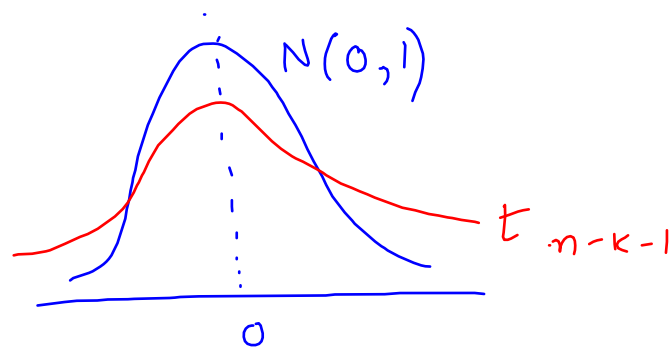
↳ from Ch. 3

$$\frac{\hat{\beta}_j - \beta_j}{sd(\hat{\beta}_j)} \sim N(0, 1)$$

$$\frac{\hat{\beta}_j - \beta_j}{se(\hat{\beta}_j)} \sim t_{n-k-1} \quad (\text{t dist. with } df = n-k-1)$$

\swarrow
 using $\hat{\sigma}$
 instead of σ

$\rightarrow N(0, 1)$ as $df \rightarrow \infty$



Single hyp. - single parameter

Null : $H_0 : \beta_j = a_j$ $a_j = 0 \rightarrow$ special case

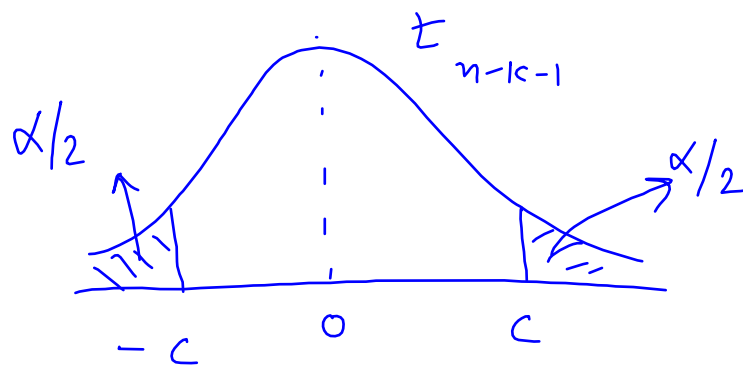
Alternative : $H_1 : \beta_j \neq a_j$

\hookrightarrow can have $>$
 $<$

Test statistic

(t " ratio)

$$t_{\text{test}} = \frac{\hat{\beta}_j - a_j}{\text{se}(\hat{\beta}_j)}$$



Reject H_0 if $|t_{\text{test}}| > c$
 else fail to reject.

$$\begin{aligned} \text{area} \square &= \alpha \\ \alpha &= P(\text{rej. } H_0 \mid H_0 \text{ true}) \\ &= \text{sig. level} \\ &\quad (\text{size}) \\ &= P(\text{Type I error}) \end{aligned}$$